



## Overview

- Production Function Parameters
- Applied Model Calibration



## Production Function Parameters

$$Y = \left\{ \alpha [(K^{sk} L^{sl})^\rho + \beta (E^{se} P^{sp} S^{ss})^\rho] \right\}^{1/\rho}$$

$\alpha, \beta$ : distribution parameters  $> 0$

- ✓ The partial derivative of this function with respect to capital represents the marginal productivity of capital
- ✓ Define the labor force index in the base year as  $L=1$  and substitute all other base year values  $\rightarrow \alpha$
- ✓ Substitute all factor and gross production values into the production function  $\rightarrow \beta$



## Production Function Parameters

$$Y = \left\{ \alpha [(KD^{skd} KF^{skf})^{sk} L^{sl}]^\rho + \beta INT^\rho + (1 - \alpha - \beta) [E^{se} P^s P S^{ss}]^\rho \right\}^{1/\rho}$$

$\alpha, \beta$ : distribution parameters  $> 0$

- ✓ The partial derivative of this function with respect to KD represents the marginal productivity of capital
- ✓ Define the labor force index in the base year as  $L=1$  and substitute all other base year values  $\rightarrow \alpha$
- ✓ The partial derivative of this function with respect to P represents the price of oil
- ✓ Substitute all other base year values  $\rightarrow \beta$

## Production Function Parameters

$$Y = A \left[ \alpha (K^{KPVS} L^{1-KPVS})^{\frac{\sigma-1}{\sigma}} + (1 - \alpha) E^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$

Nonlinear least squares (NLS) regression. The non-linear solution to the estimation problem of the parameters, will come through the minimization of the following sum of squares,  $S(A, \alpha, \sigma)$

$$S(A, \alpha, \sigma) = \frac{1}{2} \sum_{t=1988}^{2014} e_t^2$$

$$S(A, \alpha, \sigma) = \frac{1}{2} \sum_{t=1988}^{2014} \left[ Y_t - A \left[ \alpha (K_t^{KPVS} L_t^{1-KPVS})^{\frac{\sigma-1}{\sigma}} + (1 - \alpha) E_t^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}} \right]^2$$

Application on Turkish data: Küçük, M, Kumbaroğlu, G., Sarıca, K. (2018). Substitution elasticities in an energy-augmented CES production function: An empirical analysis for Turkey, *Journal of Economics and Political Economy*, Vol.5(2), pp.234-249.



## Production Function Parameters

Temple, J. (2012). The calibration of CES production functions, *Journal of Macroeconomics*, Vol.34(2).

## Applied Aggregate Economic Equilibrium Modeling

